

1 Automated Construction of Security Integrity Wrappers for
2 Industry 4.0 Applications

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7 **Abstract**

8 Industry 4.0 (I4.0) refers to the trend towards automation and data exchange in man-
9 ufacturing technologies and processes which include cyber-physical systems, where the
10 internet of things connect with each other and the environment via networking. This
11 new connectivity opens systems to attacks, by, *e.g.*, injecting or tampering with mes-
12 sages. The solution supported by communication protocols such as OPC-UA is to sign
13 and/or encrypt messages. However, given the limited resources of devices and the high
14 performance requirements of I4.0 applications, instead of applying crypto algorithms
15 to all messages in the network, it is better to focus on the messages, that if tampered
16 with or injected, could lead to undesired configurations.

17 This paper describes a framework for developing and analyzing formal executable
18 specifications of I4.0 applications in Maude. The framework supports the engineering
19 design workflow using theory transformations that include algorithms to enumerate
20 network attacks leading to undesired states, and to determine wrappers preventing these
21 attacks. In particular, given a deployment map from application components to devices
22 we define a theory transformation that models execution of applications on the given
23 set of (network) devices. Given an enumeration of attacks (message flows) we define a
24 further theory transformation that wraps each device with policies for signing/signature
25 checking for just those messages needed to prevent the attacks.

26 In addition, we report on a series of experiments checking for attacks by a bounded
27 intruder against variations on a Pick-n-Place application, investigating the effect of
28 increasing bounds or increasing application size and further minimizing the number of
29 messages that must be signed.

30 *Key words:* Industry 4.0, bounded intruder, function block, theory transformation,
31 security, safety, verification, policy, Maude, rewriting logic.

32 **1. Introduction**

33 Manufacturing technologies and processes are increasingly automated with highly
34 interconnected components that may include simple sensors and controllers as well as
35 cyber-physical systems and the Internet of Things (IoT) components. This trend is
36 sometimes referred to Industry 4.0 (I4.0). Among other benefits, I4.0 enables process

37 agility and product specialization. This increase of interconnectivity has also enabled
38 cyber-attacks. These attacks can lead to catastrophic events possibly leading to material
39 and human damages. For example, after an attack on a steel mill, the factory had to
40 stop its production leading to great financial loss¹.

41 A recent report from the *Bundesamt für Sicherheit in der Informationstechnik* (BSI)
42 on the security of Open Platform Communication Unified Architecture (OPC UA) (ma-
43 chine to machine communication protocol for industrial automation) [12], points out
44 that the lack of signed and encrypted messages on sensitive parts of the factory net-
45 work can lead to high risk attacks. For example, attackers can inject or tamper with
46 messages, confusing factory controllers and ultimately leading to a stalled or fatal state.

47 Cryptographic signing provides message integrity thus enabling systems to defend
48 against tampering and injection attacks. Message signing, however, is a computationally
49 expensive operation². Moreover, many I4.0 applications, like motion control, re-
50 quire the movement of components to synchronize in a microsecond range³. To achieve
51 both performance and security requirements, more powerful (and thus expensive) hard-
52 ware may be required, *e.g.*, CPUs that have built-in hardware encryption. Therefore,
53 instead of requiring all messages to be signed, it is much better to only sign the mes-
54 sages that when not protected could be modified or injected by an intruder to lead to an
55 undesirable situation. This leads to the question of how to determine critical commu-
56 nications.

57 To answer this question, we use formal methods to reason about I4.0 specifications
58 developed using Model-based System Engineering approach (MBSE). MBSE has been
59 advocated for the development of embedded systems also for I4.0 applications through
60 the standard IEC 61499 [28, 27]. Following this approach, embedded systems are
61 developed by decomposing and implementing system functions into a collection of
62 communicating function blocks. A function block is an executable model of a function
63 between inputs variables and outputs variables. The behavior of function blocks are
64 specified by using executable models, such as state machines. Existing tools, such
65 as 4diac⁴ and AutoFOCUS⁵, support the development of I4.0 systems, including the
66 specification of function blocks using state machines, automated code generation from
67 these specifications, and deployment into devices. However, there has been little focus
68 on the formal analyses of such applications, in particular, on how attacks can lead to
69 harm and how to avoid such attacks.

70 This paper presents a formal framework for specifying I4.0 applications following
71 this MBSE approach and analyzing safety and security properties using Maude [8].
72 The engineering development process from application design and testing to systems
73 deployment is captured by theory transformations with associated theorems showing

¹https://www.bsi.bund.de/SharedDocs/Downloads/DE/BSI/Publikationen/Lageberichte/Lagebericht2014.pdf?__blob=publicationFile

²<https://medium.com/logos-network/benchmarking-hash-and-signature-algorithms-6079735ce05>

³<http://www.hit.bme.hu/~jakab/edu/litr/TimeSensNet/TSN-Time-Sensitive-Networking-White-Paper.pdf>

⁴<https://www.eclipse.org/4diac/>

⁵<https://www.fortiss.org/en/results/software/autofocus-3>

74 that results of analysis carried out at the abstract application level hold for models of
75 deployed systems.

76 Our key contributions are as follows:

77 • **I4.0 Application Behavior:** We present a formal executable model of the behavior
78 of I4.0 applications in the rewriting logic system Maude [8]. An application is
79 composed of interacting state transition machines which, following the IEC 61499
80 standard [27], we call function blocks.

81 • **Bounded Symbolic⁶ Intruder Model:** The security verification problems that
82 we consider are undecidable in general, but decidable PSPACE-complete if we
83 bound the number of messages that the intruder can inject or tamper [1]. Using
84 the number of messages an intruder can inject/tamper can be used as a metric for
85 the level of security of I4.0 applications. The greater the number of messages that
86 intruder can inject or tamper, the greater is his attack power. Indeed, any attack
87 using n messages can be performed by an attacker capable of injecting/tampering
88 $m \geq n$ messages. Therefore, showing that an intruder with n messages is not
89 able to carry out an attack provides a form of quantitative assurance on the level of
90 security of the system.

91 We use this fact to evaluate the security of an application, we formalize a fam-
92 ily of bounded intruders parameterized by the number of messages the intruder
93 can inject. Our intruder can generate any message that is not encrypted, but can
94 not generate (or read) messages signed by honest devices. To reduce state space
95 complexity the intruder model is converted to one in which messages are *symbolic*
96 and are instantiated opportunistically according to what can be received at a given
97 time. Using search in the resulting symbolic model all intruder message sets that
98 can lead to a bad state can be enumerated. Each such message defines a flow be-
99 tween two function blocks that must be protected. Proof of the *Intruder Theorem*
100 shows that the concrete and symbolic intruder models yield the same attacks.

101 • **Deployment transformation:** The application model is suited to reason about
102 functionality and message flows. Such applications models are deployed into a
103 system architecture, composed by hardware units and communication mediums.
104 Accordingly, we define a theory transformation from an application executable
105 specification to a specification of a deployment of that application using a map
106 from application function blocks to a given set of devices. Proof of the *Deployment*
107 *Theorem* shows that in the absence of intruders, applications and their deployments
108 satisfy the same function block based properties. Proof of the *Deployment Intruder*
109 *Theorem* shows that any bounded intruder attack at the system level can be found
110 already at the application level. Thus one can carry out security verification at the
111 application level as the results can be transferred to deployed applications.

112 • **Security Integrity Wrappers:** Use of security wrappers is a mechanism to protect
113 communications [7]. Here it is used to secure message integrity between devices
114 using signing. Since signing is expensive, it is important to minimize message

⁶Throughout this paper we use the terminology *symbolic* to indicate the use of symbols (variables) in representations of model entities such as messages, executions, and analyses. This allows compact representation of the state space and enables formal analysis of non-trivial systems.

115 signing. We define a transformation from a specification of a deployed application
116 to one in which devices are wrapped with a policy enforcement layer where the
117 policies are computed from a set of message flows that must be protected as deter-
118 mined by the enumeration of possible attacks. The proof of the *Wrapping Theorem*
119 shows that the wrapping transformation protects the deployed system against iden-
120 tified attacks.

121 • **Minimal protection set.** In the case that there are multiple attacks it is only nec-
122 essary to protect one message from each attack, not all messages from all attacks.
123 We introduce the notion of *minimal protection set* and present an algorithm for
124 computing such sets. Thus further improving the efficiency of wrapping policies.

125 We have implemented the framework and carried out a number of experiments
126 demonstrating the analysis, deployment, and wrapping for variations of a PickNPlace
127 application. The Maude code along with documentation, scenarios, sample runs and
128 a technical report with details and proofs can be found at <https://github.com/SRI-CSL/WrapPat.git>. An early version of the framework was presented in [21]
129 where we demonstrated the use of the search command to find logical defects and
130 enumerate attacks, and proposed the idea of device wrappers. That paper contains a
131 number of experiments, including scalability results. In an another co-joint paper [1],
132 we investigated the complexity of security verification problems involving bounded
133 intruders and extends the experiments with four selected scenarios constructed from
134 the example described in Section 2.1. This paper is an extension of our WRLA20
135 workshop paper [22]. The new contributions in the workshop paper included the the-
136 orems and proofs, implementation of the deployment and wrapping functions, and a
137 simplified version of the symbolic intruder model. Moreover, Section 4.2 defines the
138 new concept of minimal protection set that contains the messages that are enough to
139 be signed by security wrappers to ensure security (under the assumptions on the given
140 intruder model). We propose an algorithm to compute this minimal set and apply it to
141 the four examples described in Section 4. With this new concepts, we refine security
142 wrappers reducing the number of messages to be encrypted as compared to our previ-
143 ous work [22] while still ensuring security. Depending on the scenario this reduction
144 can be of more than 50% of messages when compared to the approach in [22].

145 **Plan:** Section 2 gives an overview of technical ideas and theorems, and describes
146 a motivating example, which will be used as a running example in the paper. Section 3
147 presents the formalization of our I4.0 framework and bounded attack model in Maude:
148 the application level, the deployment and security wrapper transformations, and theo-
149 rems characterizing the guarantees of the transformations. Section 4 describes how our
150 machinery supports automated reasoning. It also shows how to improve the efficiency
151 of the security wrapper. Section 5 discusses related work, and Section 6 concludes with
152 ideas for future work.
153

154 2. Overview

155 *Threat Model.* We assume that devices have their pair of secret and public keys. More-
156 over, that devices can be trusted and that a secret key is only known by its corresponding
157 device. However, the communication channels shared by devices are not trusted. An

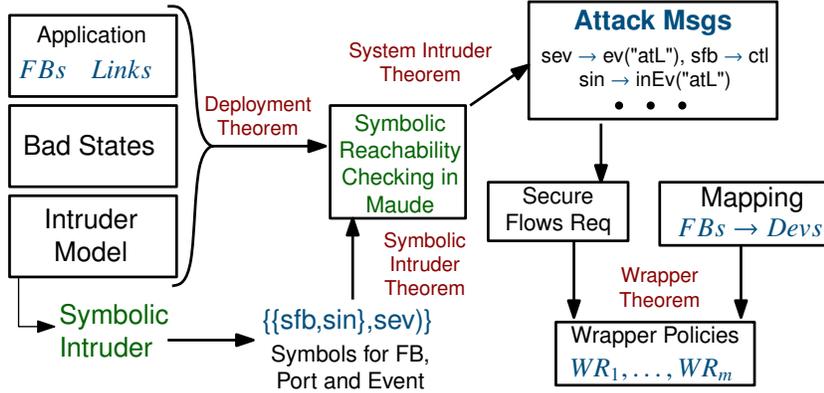


Figure 1: Methodology Overview

158 intruder can, for example, inject and tamper with (unsigned) messages in any commu-
 159 nication channel. This intruder model reflects the critical types of attacks in Industry
 160 4.0 applications as per the BSI report [12].

161 To protect communications between function blocks on different devices we use the
 162 idea of formal wrapper [7] to transform a system S into a system, $wrap(S, emsgs)$,
 163 in which system devices are wrapped in a policy layer protecting communications be-
 164 tween devices by signing messages and checking signatures on flows. Intuitively, a
 165 security integrity wrapper enforces a policy that specifies which incoming events a de-
 166 vice will accept only if they are correctly signed and which outgoing events should be
 167 signed. By using security integrity wrappers it is possible to prevent injection attacks.
 168 For example, if all possible incoming events expected in a device are to be signed, then
 169 any message injected by an intruder would be rejected by the device. However, more
 170 messages in security integrity wrappers means greater computational and network over-
 171 head. One goal of our work is to derive security integrity wrappers, WR_1, \dots, WR_n ,
 172 for devices, Dev_1, \dots, Dev_n in which software, called function blocks, are to be ex-
 173 ecuted, to ensure the security of an application while minimizing the number of events
 174 that must be signed.

175 Figure 1 depicts the key components in achieving this goal with the inputs:

- 176 • **Application (App):** a set, $\{FB_1, \dots, FB_n\}$, of function blocks (FBs) and links,
 177 *Links*, between output and target input ports. An FB is a finite state machine
 178 similar to a Mealy Machine [18]. An App executes its function blocks in cycles.
 179 In each cycle, the input pool is delivered to function block inputs and each function
 180 block fires one transition if possible. The remaining inputs are cleared, the function
 181 block outputs are collected, routed along the application links, and stored in the
 182 application input pool.
- 183 • **Bad State:** a predicate (*badstate*) specifying which combined FB states should
 184 be avoided, for example, states that correspond to catastrophic situations.
- 185 • **Intruder Capabilities:** The intruder is given a set of all possible messages deliv-
 186 erable in the given application. For up to n times the intruder can pick a message
 187 from this set and inject it into the application input pool at any moment of execu-
 188 tion.

189 We use a symbolic representation of intruder messages and Maude’s search capability
 190 to determine which messages, called *attack messages*, that an intruder can inject to

191 drive the system to a bad state. FBs are finite state machines that either get stuck or
192 are periodic. Therefore, since there is a bounded number of FBs in an application, the
193 overall state-space is finite. This means that, due to Maude’s in built memoization,
194 search always terminate provided there is enough memory. We extract the critical
195 events, *i.e.*, injected message sets leading to a bad state, from attack traces of a given
196 an application in a symbolic intruder environment. This is done by using Maude’s
197 reflection features enabling one to manipulate with search traces.

198 Deploying an application can be seen as a theory transformation [20]. The function
199 `deployApp` takes an application and a deployment mapping from FBs to devices and
200 returns a system model that is the deployed version of the application corresponding to
201 the mapping.

202 From the enumerated attack messages, we derive which flows between function
203 blocks on different devices need to have their events signed. Finally, from these flows,
204 we are able to derive the security integrity wrapper policies for a given mapping of
205 function blocks to devices.

206 Notice that we are able to capture multi-stage attacks, where the system is moved
207 to multiple configurations before reaching a bad state. This is done by using stronger
208 intruders that can use a greater number of messages.

209 *Challenges.* To achieve our goal, we encounter a number of challenges.

- 210 • **Challenge 1 (Deployment Agnostic):** As pointed out above, the deployment of
211 FBs on devices can affect the security requirements of flows. Analysis at the sys-
212 tem level is more complex than at the application level. Thus it is important to
213 understand how analysis on the application level can be transferred to the system
214 level.
- 215 • **Challenge 2 (Symbolic Intruder):** Our intruder may inject a given set of concrete
216 messages and a bound n on the number of injections. The search space grows
217 rapidly with the bound. To reduce the search space, the concrete messages and
218 bound n is replaced by n distinct symbolic messages. The symbols are instantiated
219 only when required. The challenge is to ensure the soundness and completeness of
220 symbolic search. That is, an execution using the symbolic model corresponds to at
221 least one execution using the concrete model and vice-versa.
- 222 • **Challenge 3 (Complete Set of Attack Messages):** Given an intruder, how do we
223 know that at the end the set of attack messages found is a complete set for any
224 deployment?
- 225 • **Challenge 4 (System Security by Wrapping):** How do we know that the wrap-
226 pers constructed from identified flows and deployment mapping ensure the security
227 of the system assuming our threat model?

228 To address these challenges, we prove the following theorems:

229 **Symbolic Intruder Theorem (Theorem 3.1)** states that each execution of an applica-
230 tion A in a symbolic intruder environment has a corresponding execution of A in the
231 concrete intruder environment with the same bound, and conversely. The key to this
232 result is the soundness and completeness of the symbolic match generation.

233 **Deployment Theorem (Theorem 3.3)** states that executions of an application A and a
234 deployment S of A are in close correspondence. In particular, the underlying function

235 block transitions are the same and thus properties that depend only on function block
236 states are preserved.

237 **System Intruder Theorem (Theorem 3.5)** states that, letting A, S be as in the De-
238 ployment Theorem, (1) for any execution of S in an intruder environment there is a
239 corresponding execution of A in that environment; and (2) for any execution of A in
240 an (concrete or symbolic) intruder environment that does not deliver any intruder mes-
241 sages that should flow on links internal to some device, has a corresponding execution
242 from S in that environment. Corresponding executions preserve attacks and FB proper-
243 ties. The condition in part (2) is because internal messages are protected by the device
244 execution semantics.

245 **Wrapper Theorem (Theorem 3.7)** Let A be an application, S a deployment of A ,
246 and $msgs$ a set of messages containing the attack messages enumerated by symbolic
247 search with an n bounded intruder. The wrapper theorem says that the wrapped system
248 $wrap(S, msgs)$ is resistant to attacks by an n bounded intruder.

249 *Remark:*. The formal machinery developed in this paper is to enable early verifica-
250 tion of applications by identifying (minimal) requirements on which messages shall be
251 protected by means of security wrappers. These requirements shall be used during the
252 development in implementation decisions, such as the computational power of devices,
253 or whether specialized Hardware Security Modules with Hardware Encryption shall be
254 used to increase the efficiency of encryption. For example, it has been shown that more
255 expensive CPUs with in built hardware encryption are up to six times faster than CPUs
256 without in built hardware encryption.⁷ Furthermore, these requirements may guide the
257 deployment of FBs on devices if one assumes that the connection between FBs in the
258 same device are implicitly secure. Indeed, these requirements can be used together
259 with design space exploration [25] techniques.

260 2.1. Example

261 Consider an I4.0 unit, called Pick and Place (PnP),⁸ used to place a cap on a cylin-
262 der. The cylinder moving on the conveyor belt is stopped by the PnP at the correct
263 location. Then an arm picks a cap from the cap repository, by using a suction mech-
264 anism that generates a vacuum between the arm gripper and the cap. The arm is then
265 moved, so that the cap is over the cylinder and then placed on the cylinder. Finally, the
266 cylinder with the cap moves to the next factory element, *e.g.*, storage element.

267 Following the IEC 61499 standard [27]. Model-Based System Engineering (MBSE)
268 tools, such as 4diac⁹, specify such Industry 4.0 by using function blocks. A function
269 block is an executable specification, typically a Mealy machine, and an application
270 is a collection of communicating function blocks. From these specifications, existing
271 MBSE tools generate code that can be deployed in the devices used in factory.

⁷<https://www.tomshardware.com/reviews/clarkdale-aes-ni-encryption,2538-5.html>

⁸See <https://www.youtube.com/watch?v=Tkcv-mbhYqk> starting at time 55 seconds for a very small scale version of the PnP.

⁹<https://www.eclipse.org/4diac/>

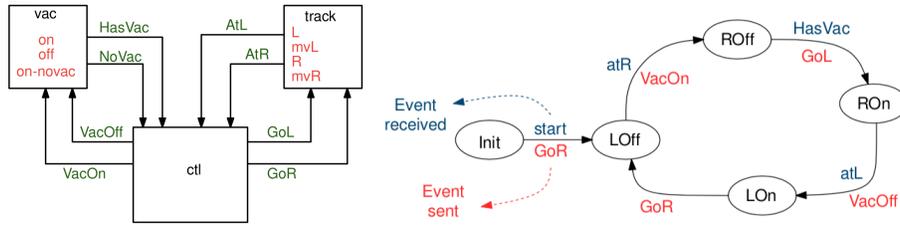


Figure 2: PnP Function Blocks, *ctl*, *vac*, and *track*. The internal states of *vac* and *track* are shown in their corresponding boxes and their transitions are elided. The complete specification is shown in the finite machine to the right.

272 An application implementing the PnP logic has three function blocks (FBs) that
 273 communicate using the channels as shown in Figure 2. The controller, *ctl*, coordinates
 274 with the *vac* and *track* function blocks as specified by the finite machine in Figure 2.
 275 For example, after starting, it sends the message *GoR* to the *track* that then moves to
 276 the right-most position (state *mvR*) where the caps are to be picked. When the *track*
 277 reaches this position, it informs the controller by sending the message *AtR*. *ctl* then
 278 sends the message *VacOn* to the *vac* function block that starts its vacuum mechanism.
 279 If a vacuum is formed indicating that a cap has been picked, *vac* sends the message
 280 *on-hasVac* to *ctl*. *ctl* then sends *GoL* to the *track*. This causes the *track* to move to
 281 the left-most position (state *mvL*) where the cylinder is located and on which the cap
 282 has to be placed. The *track* sends the message *AtL*. *ctl* then sends the message *VacOff*
 283 to the *vac* to turn off the vacuum mechanism causing the cap to be placed over the
 284 cylinder.

285 As illustrated by the PnP execution above, the execution of applications is assumed
 286 to be synchronous. That is, a global execution cycle, also called hypercycle, only
 287 ends when all FBs have executed their steps. This is normally achieved by using a
 288 time synchronization protocol. In particular, FBs execute internally generating events
 289 which are then communicated to other FBs to be processed in the next global cycle.
 290 Finally, we also point out that FBs may also exchange data and not only events. These
 291 data communication channels may contain sensitive data that shall be protected. In
 292 this paper, we do not consider such attacks, but only attacks from the manipulation of
 293 event links. Notice that these events do not possess any complex structure being simple
 294 constants.

295 For larger scale PnP, the hazard “Unintended Release of Cap” is catastrophic, for
 296 example picking bricks rather than caps, as dropping a brick can hurt someone that
 297 is near the PnP. By performing analysis, such as STPA (Systems-Theoretic Process
 298 Analysis)¹⁰, one can determine that this event can occur when *The track function block*
 299 *is at state mvL and the vac function block is in state on-novac or in state off*. This
 300 is because when starting to move to the position to the left, the gripper may have
 301 succeeded to grab a cap. However, while the arm is moving, the vacuum may have

¹⁰https://psas.scripts.mit.edu/home/get_file.php?name=STPA_handbook.pdf

302 been lost causing the cap to be released, *i.e.*, the `vac` function block is in state `on-`
 303 `novac` or `off`. An intruder can cause such an event by injecting the message `VacOff` to
 304 the `vac` when the arm is moving left, that is, in state `mvL`, while the gripper is holding
 305 something.

306 Following our methodology, shown in Figure 1, we feed to our Symbolic Reachability-
 307 Checker the PnP function blocks, its bad state above, and a symbolic intruder that can
 308 inject at most one message. One can specify stronger intruders, but this weak intruder is
 309 already able to lead the system into a bad state. Indeed, from the reachability-checker's
 310 output, we find that there are four different attack messages. One of them is shown in
 311 Figure 1, where the intruder impersonates the `track` and sends to the `ctl` a message `AtL`
 312 while the `track` is still moving.

313 From the identified attack messages we can see that messages in the flow from the
 314 `track` to the `ctl` involving the message `AtL` should be protected.

315 Suppose `track` and `ctl` are deployed in dev_1 and dev_2 , respectively, then the com-
 316 puted security integrity wrapper on dev_1 will sign `AtL` messages, and the security in-
 317 tegrity wrapper on dev_2 will check whether `AtL` messages are signed by dev_1 . If `track`
 318 and `ctl` are deployed on the same device, there is no need to sign `AtL` messages as we
 319 trust devices to protect internal communications.

320 3. Formalization of the I4.0 framework in Maude

321 We now describe the formal representation of applications, and the deployment and
 322 wrapping transformations. We formalize theorems. We describe the main structures,
 323 operations, and rules using snippets from the Maude specification. Examples come
 324 from the Maude formalization of the PnP application of Section 2.

325 3.1. Function blocks

326 An I4.0 application is composed of a set of interconnected interactive finite state
 327 machines called function blocks. A function block is characterized by its finite set of
 328 states, finite sets of inputs and outputs, a finite set of possible events at each input or
 329 output, and a finite set of transitions. We call this characterization a FB class. To allow
 330 for multiple occurrences of a given FB class in an application the state of a FB has both
 331 an instance and a class identifier. The events communicated among function blocks do
 332 not have any complex structure being constants.

333 The Maude representation of a FB is a term of the form $[fbId : fbCid |$
 334 $fbAttrs]$, where $fbId$ is the FB identifier, $fbCid$ its class identifier and $fbAttrs$
 335 is a set of attribute-value pairs, including $(state : st)$, $(iEvEfts : ieffs)$,
 336 $(oEvEfts : oeffs)$, and $(ticked : b)$, with $state$, $iEvEfts$, $oEvEfts$,
 337 $ticked$ being the attribute tags, st the current state, $ieffs$ a set of signals/events to
 338 be processed (incoming effects), $oeffs$ a set of signals/events to be transmitted (out
 339 effects), and b a boolean indicating whether the FB has fired a transition in the current
 340 cycle.

341 A transition is a term of the form $tr(st0, st1, cond, oeffs)$ where $st0$ is
 342 the initial state and $st1$ the final state, $cond$ is the condition, and $oeffs$ is the set
 343 of outputs of the form $o : \sim ev$ specifying that the event ev is to sent on the output

344 port o . A condition is a boolean combination of primitive conditions (in is ev)
 345 specifying a particular event (ev) at input in . $tr(st0, st1, cond, oeffs)$ is a
 346 transition enabled by a set of inputs if they satisfy $cond$ and the current state of the
 347 function block state $st0$. In this case, the transition can fire, changing the function
 348 block state to $st1$ and emitting $oeffs$.

349 *Example FB.* The FB with class identifier vac has states

```
st("off"), st("on"), st("on-novac");
```

350 inputs

```
inEv("VacOn"), inEv("VacOff");
```

352 outputs

```
outEv("NoVac"), outEv("HasVac").
```

354 The initial state, $vacInit(id("vac"))$, of an FB with class vac and identifier
 355 $id("vac")$ is

```
[id("vac") : vac | state : st("off") ; ticked : false ;  
iEvEffe : none ; oEvEffe : none]
```

358 The function $trsFB(fbCid)$ returns the set of transitions for function blocks of class
 359 $fbCid$. $trsFB(fbCid, st)$ selects the transitions in $trs(fbCid)$ with initial
 360 state st . For example $trsFB(vac, st("off"))$ returns three transitions

```
tr(st("on"), st("off"), inEv("VacOff") is ev("VacOff"),  
outEv("NoVac") :~ ev("NoVac"))  
tr(st("off"), st("on-novac"), inEv("VacOn") is ev("VacOn"),  
outEv("NoVac") :~ ev("NoVac"))  
tr(st("off"), st("on"), inEv("VacOn") is ev("VacOn"),  
outEv("HasVac") :~ ev("HasVac"))
```

We compile a transition condition into a representation as a set of constraint sets. We can think of a constraint set (CSet) as a finite map from function block inputs to finite sets of events. A set of inputs $ieffs = \{(in_i \triangleright ev_i) | 1 \leq i \leq k\}$ satisfies a CSet, $cset$, just if $cset$ has size k , the in_i form a set equal to the domain of $cset$, and ev_i is in $cset(in_i)$ for $1 \leq i \leq k$. The function $condToCSet(cond)$ returns the set of CSets such that an input set satisfies some CSet in the result just if it satisfies $cond$. Here is the idea. Let $condF = DNF(NNF(cond))$ be the disjunctive negative normal form of $cond$. $condF$ is a disjunction of clauses (conjunctions) whose elements have the form $(in$ is $ev)$ or $not(in$ is $ev)$. Since the set of possible values of ev is finite, call it $allE$, we allow the second component of $(in$ is $ev)$ to be a set and replace $not(in$ is $ev)$ by $(in$ is $allE - ev)$. Then, for each clause we replace the set of constraints for a given input, in , by the intersection of the associated event sets. This preserves satisfiability since the I4.0 model delivers at most one event on each input when a transition fires, so a conjunction demanding two or more events on an input is not satisfiable. Next remove any clauses containing a conjunct $(in$ is $empty)$ as they are unsatisfiable. The remaining disjuncts are converted to maps

such that `(in is evs)` maps `in` to the set `evs`. This is the set of constraint sets `condToCSet (cond)`. For the `vac` example, the CSet

```
condToCSet ( inEv("VacOn") is ev("VacOn"))
```

361 maps `inEv("VacOn")` to the singleton `ev("VacOn")`. As another example, a
 362 condition that captures the constraint that `track` requires messages from both `ctl`
 363 and `vac` to move left is

```
364 (inEv("GoL") is ev("GoL")) and
365 ((inEv("HasVac") is ev("HasVac")) or
366 (inEv("noVac") is ev("noVac")))
```

367 Its disjunctive normal form is

```
368 (inEv("GoL") is ev("GoL")) and (inEv("HasVac") is ev("HasVac"))
369 or
370 (inEv("GoL") is ev("GoL")) and (inEv("noVac") is ev("noVac"))
```

371 Thus the result of applying `condToCSet` to this condition is two CSets: one maps
 372 `inEv("GoL")` to `ev("GoL")` and `(inEv("HasVac")` to `ev("HasVac")`; and
 373 the other maps `inEv("GoL")` to `ev("GoL")` and `(inEv("noVac")` to `ev("noVac")`.
 374 The function `condToCSet` is lifted to transitions by the function

```
375 tr2symtr(tr(st1, st2, cond, oeffs)) =
376 symtr(st1, st2, condToCSet (cond), oeffs) .
```

377 3.2. Application structure and semantics

378 An application term has the form `[appId | appAttrs]`. Here `appAttrs` is a
 379 set of attribute-value pairs including `(fbs : funBs)` and `(iEMsgs : emsgs)`,
 380 where `funBs` is a set of function blocks (with unique identifiers), and `emsgs` is the
 381 set of incoming messages of the form `{{fbId, in}, ev}`.

382 We use `fbId`, `fbId0 ...` for FB identifiers, `in/out` for FB input/output connec-
 383 tions, and `ev` for the event transmitted by a message. Terms of the form `{fbId, in/out}`
 384 are called Ports. For entities `X` with attributes, we write `X.tag` for the value of the at-
 385 tribute of `X` with name 'tag'.

386 The initial state of the PickNPlace (PnP) application described in Section 2 is

```
387 [id("pnp") | fbs : (ctlInit(id("ctl"))
388 trackInit(id("track")) vacInit(id("vac")));
389 iEMsgs : {{id("ctl"), inEv("start")}, ev("start")};
390 oEMsgs : none ; ssbs : none]
```

391 where the message `{{id("ctl"), inEv("start")}, ev("start")}` starts the
 392 application controller.

393 Links of the form `{{fbId0, out}, {fbId1, in}}` connect output ports of one
 394 FB to inputs of another possibly the same FB. They also connect application level
 395 inputs to FB inputs and FB external outputs to application level outputs. In a well

396 formed application, each FB input has exactly one incoming link.¹¹ In principle the
 397 link set is an attribute of the application structure. In practice, since it models fixed
 398 ‘wires’ connecting function block outputs and inputs and does not change, to avoid
 399 redundant information in traces, we specify a function `appLinks (appId)` which is
 400 defined in application specific scenario modules.

401 As an example, here are the two links that connect `vac` outputs to controller inputs.

```
402     {{id("vac"),outEv("NoVac")}, {id("ctl"),inEv("NoVac")}}
403     {{id("vac"),outEv("HasVac")},{id("ctl"),inEv("HasVac")}}
```

404 *Application Execution Rules.* There are two execution rules for application behavior
 405 and two rules modeling bounded intruder actions, one for the concrete case and one for
 406 the symbolic case. To ensure that an FB fires at most one transition per cycle, each FB
 407 is given a boolean `ticked` attribute, initially `false`, which is set to `true` when a
 408 transition fires, and reset to `false` when the outputs are collected.

409 The following two rules specify the nominal semantics of I4.0 applications, *i.e.*,
 410 without the presence of intruders. The first rule, `[app-exe1]`, specifies the internal
 411 execution of a FB, while the second rule, `[app-exe2]`, specifies the end of a global
 412 execution when no FB can make an internal execution.

413 The rule `[app-exe1]` fires an enabled function block transition and sets the
 414 `ticked` attribute to `true`.

```
415 crl[app-exe1]:
416   [appId |
417     fbs : ([fbId : fbCid | (state : st) ;
418           (ticked : false) ; oEvEffs : none ; fbAttrs] fbs1) ;
419     iEMsgs : (emsgs0 iemsgs) ;
420     ssbs : ssbs0 ; appAttrs ]
421 =>
422   [appId |
423     fbs : ([fbId : fbCid | (state : st1) ;
424           (ticked : true) ; oEvEffs : oeffs ; fbAttrs] fbs1) ;
425     iEMsgs : iemsgs ;
426     ssbs : (ssbs0 ssbs1) ; appAttrs ]
427   if symtr(st,st1,[css] csss,oeffs) symtrs := symtrsFB(fbCid,st)
428   /\ size(emsgs0) = size(csss)
429   /\ ({ssbs1} ssbss) := genSol1(fbId,emsgs0,csss) .
```

430 The function `genSol1(fbId,emsgs0,csss)` returns a set of substitutions, con-
 431 sisting of all and only substitutions that match `emsgs0` to a solution of the CSet, `csss`,
 432 *i.e.*, `genSol1` is sound and complete. Note that this could be the empty set of substi-
 433 tutions if there are no solutions. In the case of concrete messages, *i.e.*, not containing
 434 symbols, the function `genSol1` just returns an set consisting of the empty substitu-
 435 tion if `emsgs0` satisfies `csss`, while it returns an empty set of substitutions if `emsgs0`
 436 fails to satisfy `csss`. `genSol1`, equationally defined in Maude, directly implements

¹¹Otherwise, if an input port of a FB receives two different incoming links, the execution semantics of the FB is not well defined as it is not clear which incoming event from which incoming link.

437 the notion of satisfaction described above, where CSets and symbolic transitions are
 438 introduced. When rewriting, just one partition of `iemsgs`, one choice of (symbolic)
 439 transition, and one satisfying substitution is selected. Search will explore all possible
 440 choices.

441 When `[app-exe1]` is no longer applicable (`hasSol (fbs, iemsgs)` is false),
 442 `[app-exe2]` collects and routes generated output and prepares for the next cycle.

```

443 crl[app-exe2]:
444   [appId |
445     fbs : fbs ;
446     iEMsgs : iemsgs ;
447     oEMsgs : oemsgs ;
448     attrs]
449 =>
450   [appId |
451     fbs : fbs2 ;
452     iEMsgs : emsgs0 ;
453     oEMsgs : (oemsgs emsgs1) ;
454     attrs1]
455   if not hasSol(fbs, iemsgs)
456   /\ tick := notApp(attrs)
457   /\ not getTicked(attrs) --- avoid extracting when no trans
458   /\ attrs1 := setTicked(attrs, true)
459   /\ {fbs2, emsgs0, emsgs1} :=
460     extractOutMsgs(tick, fbs, none, none, none, appLinks(appId)) .

```

461 The function `extractOutMsgs` removes outputs from the function blocks that fired
 462 and routes them using `appLinks (appId)` to the linked FB input or application
 463 output. Application level inputs are accumulated in `emsgs0` and outputs are accu-
 464 mulated in `emsgs1`. The ticked attribute of each FB is set to the value of `tick`. In
 465 the case of a basic application, this will be `false` indicating the FB is ready for the
 466 next cycle. When the application level execution rules are used in a larger context,
 467 (`notApp(attrs)` is true), `extractOutMsgs` ensures that each FBs ticked attri-
 468 bute is `true`, allowing further message processing before repeating the execution
 469 cycle. If the application has a ticked attribute, it is set to `true`, to indicate it has
 470 completed the current cycle. `fbs2` collects the updated function blocks.

471 3.3. Intruders

472 An application `A` in the context of an intruder is represented in the concrete case
 473 by a term of the form `[A, emsgs, n]` where `emsgs` is a set of specific messages
 474 (typically all the messages that could be delivered) and `n` is the number of injection
 475 actions remaining. The rule `[app-intruder-c]` (omitted) selects one of the candi-
 476 date messages, injects it, and decrements the counter.

477 An application `A` in the context of a symbolic intruder is represented by a structure
 478 of the form `[A, smsgs]` where `smsgs` are symbolic intruder messages of the form
 479 `{{idSym, inSym}, evSym}`, where `idSym`, `inSym`, `evSym` are symbols stand-
 480 ing for function block identifiers, inputs, and events respectively). We require different

481 messages to have distinct symbols. The rule `[app-intruder]` selects one of the in-
 482 truder messages, and moves it from the intruder message set to the incoming messages
 483 `iEMsgs`.

```
484 rl[app-intruder]:
485 [[appId | fbs : fbs ; iEMsgs : emsgs0 ; attrs], emsg emsgs]
486 =>
487 [[appId | fbs : fbs ; iEMsgs : (emsgs0 emsg) ; attrs], emsgs] .
```

488 We note that this rule works equally well with concrete or symbolic messages, allow-
 489 ing one to explore consequences of injecting specific messages. Using `genSol1`, a
 490 symbolic message can be instantiated to any deliverable message. Also, if a message
 491 is injected after all function blocks have been ticked and before `[app-exe2]` is ap-
 492 plied, it will be dropped by `[app-exe2]`, since function block inputs are cleared
 493 before collecting the next round of inputs.

494 3.4. The Intruder Theorem

495 We define a correspondence $[A_s, \text{smsgs}] \sim [A_c, \text{cmsgs}, n]$ between sym-
 496 bolic and concrete intruder states as follows:

497 $[A_s, \text{smsgs}] \sim [A_c, \text{cmsgs}, n]$ holds only if

- 498 • $\text{size}(\text{smsgs}) = n$,
- 499 • $A_s.fbs = A_c.fbs$, and
- 500 • $(A_s.iEMsgs)[ssbs] = A_c.iEMsgs$

501 for some symbol substitution $ssbs$.¹² Two rule instances correspond if they are
 502 instances of the same rule. Also, in the `[app-exe1]` case the instances are the same
 503 transition of FBs with the same identifier, and in the `[app-exe2]` case the instances
 504 collect the same outputs.

505 An execution trace is an alternating sequence of (application) states and rule in-
 506 stances connecting adjacent states as usual. A symbolic trace TrS from $[A, \text{smsgs}]$
 507 and a concrete trace TrC from $[A, \text{emsgs}, n]$ correspond just if they have the same
 508 length and the i^{th} elements correspond as defined above.

509 **Theorem 3.1.** Let $[A, \text{smsgs}] \sim [A, \text{cmsgs}, n]$ be corresponding *initial* appli-
 510 cation states in symbolic and concrete intruder environments respectively, where no
 511 intruder messages have been injected.

512 If TrS is an execution trace from $[A, \text{smsgs}]$ then there is a corresponding exe-
 513 cution trace TrC starting with $[A, \text{cmsgs}, n]$ and conversely.

Proof. By induction on trace length. The base case is simple in either direction, since
 an intruder message is only involved if the rule is an `app-intruder` rule. Let

$$TrS = TrS_0 \rightarrow [A_{s_k}, \text{smsgs}_k] - rl_k \rightarrow [A_{s_k} + 1, \text{smsgs}_{k+1}]$$

¹²Note that the attributes `ssbs` and `oEMsgs` do not affect rule application.

be an execution trace from $[A, \text{msgs}]$. By induction, let

$$TrC_0(\text{msgs}) \rightarrow [Ac_k, \text{msgs}, n_k]$$

be the set of corresponding concrete traces from $[A, \text{msgs}, n]$ where msgs are parameters for delayed choices of injected concrete messages that remain in $iEMsgs$ (have been injected and not delivered or cleared), thus were injected since the last $[app\text{-}exe2]$ rule. If rl_k is an instance of $[app\text{-}exe1]$ then

$$As_k.iEMsgs = iemsgs = iemsgs0 \text{ emsgs0}$$

and the function block with identifier $fbId$ has a transition delivering $\text{emsgs0} [ssbs]$. Let $iemsgs0 = iemsgs00 \text{ iemsgs01}$ and $\text{emsgs0} = \text{emsgs00} \text{ emsgs01}$ where $iemsgs00, \text{emsgs00}$ are concrete and $iemsgs01, \text{emsgs01}$ are symbolic. By the correspondence, derived from the soundness of $genSol1$,

$$Ac_k.iEMsgs = iemsgs00 \text{ ipmsgs01} \text{ emsgs00} \text{ msgs01}$$

514 where $ipmsgs01 \text{ msgs01}$ are the injection message parameters such that the fol-
515 lowing equations are satisfied:

$$\text{size}(\text{msgs01}) = \text{size}(\text{emsgs01}) \quad \text{size}(\text{ipmsgs01}) = \text{size}(\text{iemsgs01})$$

Ac_k can deliver the same messages to the same function block. Let $\text{msgs01} = \text{emsgs01} [ssbs]$. We extend TrC by a applying of $[app\text{-}exe1]$ to

$$[A_{k+1}, \text{msgs00}] = [Ac_k[\text{msgs01} = \text{emsgs01} [ssbs]], \text{msgs}, n_k].$$

516 For rl_k an instance of $[app\text{-}exe2]$ or the intruder rule, TrC extends to a corre-
517 sponding trace because $[app\text{-}exe2]$ is only applied when there is no solution which
518 is preserved by the correspondence. Similarly, the symbolic execution of the intruder
519 rule is enabled if the set of intruder messages is not empty. In this case, the bound of
520 messages the intruder can inject in the concrete case will not be exceeded.

Conversely, let

$$TrC = TrC_0 \rightarrow [Ac_k, \text{msgs}_k, n_k] - rl_k \rightarrow [Ac_{k+1}, \text{msgs}_{k+1}, n_{k+1}]$$

be a concrete trace. By induction let $TrS_0 \rightarrow [As_k, \text{msgs}_k]$ be a corresponding symbolic trace. If rl_k is an instance of $cr1 [app\text{-}exe1]$ then

$$Ac_k.iEMsgs = iemsgs = iemsgs0 \text{ emsgs0}$$

and function block with identifier $fbId$ has a transition delivering emsgs0 . Let $ssbs$ be a substitution such that $As_k.iEMsgs = iemsgs' = iemsgs0' \text{ emsgs0}'$ and $\text{emsgs0}' [ssbs] = \text{emsgs0}$. By completeness of $genSol1$, $ssbs$ will be a solution generated by $genSol1$ and

$$[As_k, \text{msgs}_k] - rl_k \rightarrow [As_{k+1}, \text{msgs}_k] [Ac_{k+1}, \text{msgs}_{k+1}, n_{k+1}]$$

521 extending TrS_0 to TrS corresponding to TrC . If rl_k is an instance of [app-exe2]
 522 or an intruder rule it is easy to see that TrS_0 extends as desired.

523 **Corollary 3.2.** Search using the symbolic intruder model for paths reaching a `badState`
 524 finds all successful (bounded intruder) attacks.

525 We define the function `getBadEMsgs ([A, msgs])` that returns the set of in-
 526 jected message sets that lead to `badState`. This function uses reflection to enumerate
 527 search paths reflecting the command

```
528 search [A, msgs] =>+ appInt:AppIntruder
529     such that badState(appInt:AppIntruder) .
```

530 Since the symbols in the symbolic intruder messages are unique, the concrete messages
 531 used by the intruder to carry out an attack can be determined from the final substitution.

532 In the PnP application for an intruder with a single message, `getBadEMsgs` re-
 533 turns four attack message sets

```
534     {{{id("ctl"), inEv("HasVac")}, ev("HasVac")}}
535     {{{id("ctl"), inEv("atL")}, ev("atL")}}
536     {{{id("track"), inEv("GoL")}, ev("GoL")}}
537     {{{id("vac"), inEv("VacOff")}, ev("VacOff")}}
538
```

539 Recall from Section 2 that the PnP application state satisfies `badState` if the `track`
 540 FB is in state `st("mvL")`, presumably carrying something from right to left, and the
 541 `vac` FB is in an *off* state (`st("on-novac")` or `st("off")`).

542 3.5. Deploying an Application

543 Once an application is designed, the next step is determining how to deploy FBs on
 544 devices. We model deployment as a theory transformation, introducing a data structure
 545 to represent deployed applications, called *Systems*, extending the application module
 546 with rules to model system level communication elements, and defining a function
 547 mapping applications to their deployment given an assignment of FBs to host devices.

548 A deployed application is represented in Maude by terms of the form: `[sysId`
 549 `| appId | sysAttrs]` where `sysAttrs` is a set of attribute-value pairs includ-
 550 ing `(devs : devs)` and `(iMsgs : msgs)`. `devs` is a set of devices, and
 551 `msgs` is a set of system level messages of the form `{srcPort, tgtPort, ev}`
 552 where `srcPort/tgtPort` are terms of the form `{devId, {fbId, out/in}}`.

553 A device is represented as an application term with additional attributes including
 554 `(ticked : b)` which indicates whether all FBs have had a chance to execute. The
 555 function blocks of the application named by `appId` are distributed amongst the de-
 556 vices. The function `sysMap(sysId)` maps each FB identifier to the identifier of the
 557 device where the FB is hosted. Each device has incoming/outgoing ports corresponding
 558 to links between its function blocks and function blocks on other devices.

559 The function `deployApp(sysId, A, sysMap(sysId))` produces the deploy-
 560 ment of application `A` as a system with identifier `sysId` and FBs distributed to devices
 561 according to `sysMap(sysId)`.

```

562   ceq deployApp(sysId, app, idmap) =
563       mkSys(sysId, getId(app), devs, msgs)
564   if emsgs := getIEMsgs(app)
565   /\ devs := deployFBs(getFBs(app), none, idmap)
566   /\ msgs := emsgs2imsgs(sysId, emsgs, idmap, none) .

```

567 The real work is done by the function `deployFBs(fbs, none, idmap)` which cre-
568 ates an empty device for each device identifier in the range of `idmap` (setting `iMsgs`
569 to `none` and `ticked` to `true`). Then each FB (identifier `fbId`) of `app` is added to
570 the `fbs` attribute of the unique device identified by `idmap[fbId]`.

571 Note that the `deployApp` function can be applied to any state A_k in an execution
572 trace from A . A system S_k can be abstracted to an application by collecting all the de-
573 vice FBs in the application `fbs` attribute, collecting the `iEMsgs` attributes of devices
574 into the `iEMsgs` attribute of the application and adding system level input messages
575 to the `iEMsgs` attribute of the application (after conversion to application level).

576 The execution rules for applications apply to devices in a system. There are two
577 additional rules for system execution: `[sys-deliver]` and `[sys-collect]`.

578 The rule `[sys-deliver]` delivers messages associated to the `iMsgs` attribute. The
579 rule requires `isDone` to hold of the system devices, which means all the devices have
580 their `ticked` attribute set to `true`. The target port of a system level message identifies
581 the device and function block for delivery.

582 The rule `[sys-collect]` collects and distributes messages produced by the ap-
583 plication level execution rules. It collects application level output messages from each
584 device and converts them to system level output messages. Messages from device
585 `iEMsgs` attributes are split into local and external. The local messages are left on the
586 device, the external messages are converted to system level input messages.

We define a correspondence between execution traces from an application A , and
a deployment $S = \text{deployApp}(\text{sysId}, A, \text{idmap})$ of that application. An ap-
plication state A_1 corresponds to a system state S_1 just if they have the same func-
tion blocks and the same undelivered messages. (Note that the deployment and ab-
straction operations are subsets of this correspondence relation.) An instance of the
`[app-exe1]` rule in an application trace corresponds to the same instance of that
rule in a system trace (fires the same transition for the same function block). An in-
stance of `[app-exe2]` in an application trace corresponds to a sequence

$$\text{app-exe2+}; \text{sys-collect}; \text{sys-deliver}$$

587 in a system trace collecting and delivering corresponding messages.

588 **Theorem 3.3.** Let A be an application and $S = \text{deployApp}(\text{sysid}, A, \text{idmap})$
589 be a deployment of A . Then A and S have corresponding executions.

590 **Proof.** This is a direct consequence of the definition of corresponding traces.

591 **Corollary 3.4.** A and S as above satisfy the same properties that are based only on FB
592 states and transitions. This is because corresponding traces have the same underlying
593 function block transitions.

594 *3.5.1. Intruders at the system level*

595 Deployed applications are embedded in an intruder environment analogously to
 596 applications. We consider a simple case where the intruder has a finite set of concrete
 597 messages to inject, using it to show that any attack at the system level can already be
 598 found at the application level. A system in a bounded intruder environment is a term
 599 of the form $[sys, msgs]$ where sys is a system as above, and $msgs$ is a finite set of
 600 system level messages. The deployment function is lifted by

```
601 deployAppI (sysId, [A, emsgs], idmap) =
602   [deployApp [sysId, A, idmap], deployMsgs (emsgs, appLinks (A), idmap)]
```

603 where $deployMsgs$ transforms application level messages $\{fbport, ev\}$ to sys-
 604 tem level, $\{srcdevport, tgtdevport, ev\}$ using the link and deployment maps.

605 The intruder injection rule, $[app-intruder]$, is lifted to $[sys-intruder]$
 606 and the correspondence relation of the deployment theorem is lifted in the natural way
 607 to the intruder case.

608 **Theorem 3.5.** Assume $A_i = [A, emsgs]$ where A is an application in its initial state
 609 (no intruder messages injected) and $S_i = deployAppI (sysId, A_i, idmap)$.

- 610 1. If TrS is a trace from S_i then there is a corresponding trace from A_i .
- 611 2. If TrA is a trace from A_i that delivers no intruder messages that flow on links
 612 internal to a device, then there is a corresponding trace from S_i .

613 **Proof.** The proof is the same as for the correspondence of an application and its de-
 614 ployment. The additional condition in part 2 is needed because a device protects com-
 615 munications between FBs it hosts by having no port for delivery of such messages. In
 616 particular, if all the FBs are hosted on a single device then no intruder messages can be
 617 delivered.

618 **Corollary 3.6.** If a $badState$ is reachable from S_i then $sys2app (msgs)$ is an el-
 619 ement of $getBadEMsgs ([A, smsgs])$ where $size (smsgs) = size (msgs)$.

620 *3.6. Wrapping*

621 Towards the goal of signing only when necessary (Section 2) we define the trans-
 622 formation $wrapApp (A, smsgs, idmap)$ of deployed applications as:

```
623 wrapSys (deployApp (sysId, A, idmap), flatten (getBadEMsgs ([A, smsgs])))
```

624 where $flatten$ unions the sets in a set of sets. $wrapSys (S, emsgs)$ wraps the devices
 625 in S with policies for signing and checking signatures of messages on flows defined by
 626 $emsgs$ as described below.

627 A wrapped device has input/output policy attributes $iPol/oPol$ used to control the
 628 flow of messages in and out of the device. An input/output policy is an $iFact/oFact$
 629 set where an $iFact$ has the form $[i : fbId ; in, devId]$ and an $oFact$
 630 has the form $[o : fbId ; out]$. If $[i : fbId ; in, devId]$ is in the
 631 input policy of a device then a message $\{\{fbId, in\}, ev\}$ is accepted by that
 632 device only if ev is signed by $devId$, otherwise the message is dropped. Dually,

633 if [o : fbId ; out] is in the output policy of a device, then when a mes-
 634 sage {{fbId,out}}, ev is transmitted ev is signed by the device. Following
 635 the usual logical representation of crypto functions, we represent a signed event by a
 636 term sg(ev, devId), assuming that only the device with identifier devId can pro-
 637 duce such a signature, and any device that knows the device identifier can check the
 638 signature.

639 The function wrapSys(S, emsgs) invokes the function wrap-dev to wrap
 640 each of its devices, S.devs. In addition to the device, the arguments of this function
 641 include the set of messages, emsgs, to protect, the application links and the deploy-
 642 ment map. The links determine the sending FB, and the deployment determines the
 643 sending/receiving devices. If these are the same, no policy facts are added. Otherwise,
 644 policy facts are added so the sending device signs the message event and the receiving
 645 device checks for a signature according to the rules above.

```

646   ceq wrap-dev(dev, {{fbId,in}, ev} emsgs, links, idmap, ipol, opol)
647     = wrap-dev(dev, emsgs, links, idmap, (ipol ipoll), (opol opoll))
648   if {{fbId0,out}, {fbId,in}} links0 := links
649   /\ devId1 := idmap[fbId]
650   /\ devId0 := idmap[fbId0]
651   /\ devId1 /= devId0      ---- not an internal link
652   /\ devId := getId(dev)
653   **** if msg sent from dev add opol to sign outgoing
654   /\ opoll := (if devId == devId0
655                then [o : fbId0 ; out ]
656                else none
657                fi)
658   **** if msg rcvd by dev, require signed by sender devId0
659   /\ ipoll := (if devId == devId1
660                then [i : fbId ; in, devId0]
661                else none
662                fi) .
663
664   eq wrap-dev(dev, emsgs, links, idmap, ipol, opol) =
665     addAttr(dev, (iPol : ipol ; oPol : opol)) [owise] .
666

```

667 **Theorem 3.7.** Assume A is an application, allEMsgs is the set of all messages de-
 668 liverable in some execution of A, and smsgs is a set of symbolic messages of size
 669 n. Assume badState is not reachable in an execution of A, and emsgs contains
 670 flatten(getBadEMsgs([A, smsgs])).

- 671 1. Let wA = [wrapSys(deployApp(sysId, A, idmap), emsgs)]. Every ex-
 672 ecution from wA has a corresponding execution from A and conversely. In partic-
 673 ular badState is not reachable from wA.
- 674 2. badState is not reachable from

$$wAC = [\text{wrap}(\text{deploy}(A, \text{idmap}), \text{emsgs}), \text{allEMsgs}, n]$$

675 **Proof 1.** The proof is similar to the proof of the deployment theorem part 1, noting that
 676 by definition of the wrap function, any message in emsg will be signed by the sending

677 device and thus will satisfy the receiving device input policy and be delivered in the wA
 678 trace as it will in the A trace.

679 **Proof 2.** Assume $badState$ is reachable from wAC . Let $wAC\ rl_0 \dots rl_k\ wAC_{k+1}$ be a
 680 witness execution where $badState$ holds of wAC_{k+1} . By the assumption on A from
 681 part 1, at least one intruder message must have been delivered.

Let $\{msg_1 \dots msg_l\}$ be the intruder messages delivered in the trace, say by rules
 $rl_{j_1} \dots rl_{j_l}$. None of these messages are in $msgs$ since their events cannot be signed
 by one of the devices, and thus would not satisfy the relevant input policy. Thus there
 is a corresponding trace from the unwrapped system

$$AC = [\text{deploy}(A, \text{idmap}), \text{allEMsgs}, n]$$

682 and by the *Deploy Intruder Theorem* there is a trace from $[A, \text{allEMsgs}, n]$ reach-
 683 ing a $badState$. But $msgs$ contains all messages that are part of an intruder mes-
 684 sage set which if injected can cause $badState$ to be reached. A contradiction.

685 4. Towards Automated Reasoning

686 In the preceding sections we developed theory transformations that allow security
 687 analysis of Industry 4.0 systems to be carried out at the application level and provide
 688 automatic generation of policies and enforcement wrappers to protect against consid-
 689 ered attacks.

690 Section 4.1 reports on some proof of concept experiments described in our previ-
 691 ous work [1]. In that work, we also showed that while the security problem of deter-
 692 mining whether an intruder can lead a system to a bad state is undecidable when
 693 considering an unbounded intruder, such as the Dolev-Yao intruder [9], the problem
 694 is PSPACE-complete when considering a bounded intruder as we do here. Despite
 695 the high complexity, the proof of concept experiments demonstrate the feasibility of
 696 automated verification in realistic size systems.

697 Sections 4.2 and 4.3 introduce machinery that refines the analysis of the automated
 698 reasoning leading to the need of less messages to be protected through message sign-
 699 ing. In particular, Section 4.2 describes the refinement analysis problems addressed,
 700 and Section 4.3 introduces the formal machinery with our solution. We show its effec-
 701 tiveness by revisiting the experimental results discussed in Section 4.

702 4.1. Automated Reasoning

703 In this section we report on a series of experiments carried out in our previous
 704 work [1]. We investigated the effect of varying the intruder bound and increasing the
 705 size of the application. The experiments are based on the Maude I4.0 formalization
 706 described in [21, 22]. The scenarios analyzed are variants of a Pick-n-Place applica-
 707 tion, as described below. We use these scenarios to illustrate the analysis refinement
 708 algorithm described in Sections 4.2 and 4.3.

- 709 • (PnP) This scenario is the one described in Section 2.1.
- 710 • (2PnP) This scenario is depicted in Figure 3. It is an application containing two
 711 instances of PnP and a coordinator that ensures that the start of the cycle of each

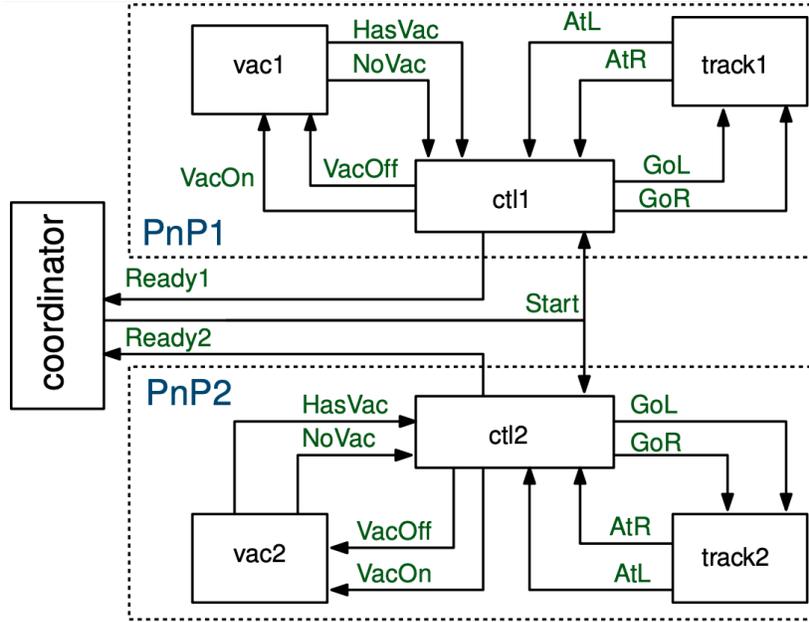


Figure 3: Illustration of the 2PnP application. This set-up has been described in [1].

712 instance of PnP happens at the same time, *i.e.*, the instance controllers send the
 713 initiating GoR at the same time.

714 • (PnP-2Msgs) This scenario modifies the logic of the PnP so that the track at the
 715 right (where the caps are) waits for two signals to head left (where the cap has to
 716 be placed): GoL from ctl and HasVac/NoVac from vac (to confirm that vac has
 717 received and processed the VacOn message); and when vac is on it requires two
 718 signals to turn off: VacOff from ctl and AtL from track. Intuitively, this means
 719 that the intruder would need at least two actions to lead this system to a bad state.

720 • (2PnP-2Msgs) This scenario is similar to the scenario 2PnP, but uses PnP-
 721 2Msgs instead of PnP.

722 For PnP/ PnP-2Msgs, *badState* holds if vac state is off or on-novac and track
 723 state is mvL. For 2PnP/2PnP-2Msgs, *badState* holds if one of the component PnP
 724 applications satisfies *badState*.

725 For each scenario, Maude search was used to check reachability of bad states in the
 726 presence of a bounded intruder with the bound on the number of intrusions between 0
 727 and 3. Note that unreachability in the bound 0 case shows that the application alone is
 728 safe with respect to the considered bad state. Table 1 summarizes experiments using
 729 the four scenarios described above.

730 These experiments show that it is feasible in practice to formally verify simple
 731 scenarios and even more complicated ones. However, as expected by the complexity
 732 results reported in [1], the computational effort increases exponentially as we increase
 733 the size of the system. Moreover, increasing the bound on intruders impacts search

Table 1: Attack search for different Pick-n-Place scenarios with bounded intruder. The values in parentheses, $\times n$, for a scenario and bound on intruder, denotes that Maude traversed n times more states than the scenario PnP with the same value for the bound on intruder. The experiments were run on a MacBook Pro, 2.4 Ghz Intel Core i5, 16GB memory. These experiments appeared in our previous work [1].

Scenario	Bound on Intruder	Number of States	Time(ms)	BadState?
PnP	0	23	4	no
	1	84	11	yes
	2	406	47	yes
	3	1651	178	yes
2PnP	0	84 ($\times 3.7$)	40	no
	1	388 ($\times 4.6$)	182	yes
	2	2873 ($\times 7.1$)	1409	yes
	3	26440 ($\times 16.0$)	19631	yes
PnP-2Msgs	0	29 ($\times 1.3$)	40	no
	1	722 ($\times 8.5$)	177	no
	2	1854 ($\times 4.6$)	912	yes
	3	10248 ($\times 6.2$)	4965	yes
2PnP-2Msgs	0	114 ($\times 4.9$)	88	no
	1	6814 ($\times 81.1$)	5277	no
	2	22179 ($\times 54.1$)	18208	yes
	3	153824 ($\times 93.1$)	225898	yes

734 as expected. Higher bound values means that intruders are capable to carry out more
735 complex attacks. For example, in the scenarios 2PnP and 2PnP-2Msgs the intruder
736 needs at least two actions to carry out an attack.

737 4.2. Analysis Refinement

738 An intruder may need to send more than one message in order to carry out an
739 attack that could lead to harm. The approach outlined in Section 2 for constructing
740 the policies of security wrappers would sign *all the messages* that the intruder could
741 use to trigger an attack. As our goal is to reduce the number of signed messages for
742 performance reasons, we investigate in this section how we could refine this analysis
743 so to reduce the number of messages required to be signed.

744 To build more refined security wrappers, we rely on the following observation: to
745 block an attack, it suffices to block the intruder to send any single message necessary
746 for carrying out the attack.

747 For example, let $\mathcal{M} = \{\text{msg}_1, \dots, \text{msg}_n\}$ be the messages necessary for carry-
748 ing out an attack. Then instead of constructing security wrappers that would sign all
749 messages $\text{msg} \in \mathcal{M}$, we can pick a non-empty subset of messages $\mathcal{M}' \subseteq \mathcal{M}$ and
750 require that the messages in \mathcal{M}' to be signed. In fact, we could pick a singleton set

751 $\mathcal{M}' = \{\text{msg}_j\}$ for some $1 \leq j \leq n$. If this message msg_j is required to be signed,
 752 then the attacker cannot complete the attack.

753 There are some problems in implementing this solution:

754 • **Problem 1:** how to compute the necessary messages, \mathcal{M} , to carry out an attack?
 755 With the approach described and implemented in Section 2, we obtain an upper
 756 bound of messages. That is, the attack message sets, \mathcal{A} , in Figure 1 may contain
 757 messages that are not strictly necessary to carry out an attack, but it does contain
 758 all messages that are necessary for carrying out an attack. Formally, $\mathcal{M} \subseteq \mathcal{A}$, but
 759 not necessarily $\mathcal{A} = \mathcal{M}$.

760 This is because of our intruder model specification. Recall that the intruder is
 761 given a fixed number, n , of (symbolic) messages that he can use to carry out an
 762 attack. If an attack can be carried out using fewer messages than available to
 763 the attacker, then the set of attack messages found by our search machinery may
 764 contain spurious messages that are not needed for carrying out the attack.

765 • **Problem 2:** There may be more than one possible attack. Therefore, our ma-
 766 chinery would find multiple sets of attack messages $\mathcal{A}_1, \dots, \mathcal{A}_m$. How can we
 767 minimize the set of message required to be encrypted while still mitigating all
 768 possible attacks?

769 In the following we show how to solve these problems.

770 4.3. Minimal Protection Sets

771 Intuitively, for each attack, it is enough to secure at least one of the messages used
 772 by the intruder to carry out that attack. We call such sets *protection sets*.

773 **Definition 4.1.** Let $\mathcal{A}_1, \dots, \mathcal{A}_n$ be the attack sets on a given system by an intruder
 774 sending at most m messages. A protection set is a set of messages such that if all
 775 messages in this set are protected then no one of the attacks corresponding to the
 776 attack sets $\mathcal{A}_1, \dots, \mathcal{A}_n$ is possible. The protection set is minimal if when any message
 777 is removed it fails to be a protection set, i.e., there is an attack.

778 For example, assume that the following attack sets:

$$\{\text{msg}_2\}, \{\text{msg}_1, \text{msg}_2\}, \{\text{msg}_1, \text{msg}_3, \text{msg}_5\}, \text{ and } \{\text{msg}_4\}. \quad (1)$$

779 The naive approach depicted in Figure 1 would lead to securing all messages in the
 780 attack sets: $\{\text{msg}_1, \text{msg}_2, \text{msg}_3, \text{msg}_4, \text{msg}_5\}$. Indeed this set is a protection set. How-
 781 ever it is not minimal as it is possible to remove msg_1 , i.e., not secure msg_1 , and the at-
 782 tacks are still not possible. The protection sets $\{\text{msg}_1, \text{msg}_2, \text{msg}_4\}$, $\{\text{msg}_2, \text{msg}_3, \text{msg}_4\}$
 783 and $\{\text{msg}_2, \text{msg}_4, \text{msg}_5\}$ are minimal.

784 We describe next an algorithm to compute minimal protection sets from the attack
 785 sets computed using the approach depicted in Figure 1.

786 Notice that the search for attacks by an intruder with n messages enumerates all
 787 attack sets \mathcal{A} such that $|\mathcal{A}| \leq n$. Let $\text{all}\mathcal{A}[n] = \{\mathcal{A} \mid \mathcal{A} \text{ is an attack set and } |\mathcal{A}| \leq n\}$.
 788 If $\mathcal{A} \in \text{all}\mathcal{A}[n]$ of size j is not minimal then there must be some $\mathcal{A}' \in \text{all}\mathcal{A}[n]$ of
 789 size $i < j$ such that $\mathcal{A}' \subset \mathcal{A}$. Thus we can reduce $\text{all}\mathcal{A}[n]$ to $\text{min}\mathcal{A}[n]$ that contains
 790 all and only minimal attack sets. A protection set is one whose intersection with each
 791 $\mathcal{A} \in \text{min}\mathcal{A}[n]$ is non-empty.

792 We compute minimal protection set for a given enumeration `asetSets` of all
 793 attacks of size $\leq n$ as follows.

Step 1: Turn the input into a list

```
asetSetsL = emsgsSet2emsgsList(asetSets)
```

794 whose j^{th} element (counting from 0) is the attack sets from `asetSets` of size $j + 1$.

Step 2: Prune the obtained list, to remove any attack set that contains an attack set of smaller size

```
asetSetsLp = pruneEMsgss(asetSetsL).
```

795 **Step 3:** From the pruned list we compute candidate minimal protection sets as fol-
 796 lows: We work with structures that are pairs `[emsgs, emsgssl]` where `emsgs` is a
 797 partial candidate protection set, and `emsgssl` is the result of removing `emsgs` from
 798 each attack set in `asetSetsLp` (and removing empty sets). Starting with the single
 799 pair `[none, asetSetsLp]`, a pair `[emsgs, emsgssl]` is processed by computing
 800 the sets `[emsgs emsg, emsgssl/emsg]` such that `emsg` is in `mxOcc(emsgssl)`
 801 and `emsgssl/emsg` is the result of removing `emsg` from each attack set in `emsgssl`
 802 (and removing empty sets). Here `mxOcc(emsgssl)` is the set of `emsgs` that occur in
 803 the maximum number of attack sets in `emsgssl`. When `emsgssl/emsg` is empty,
 804 this means all attack sets have been covered by `emsgs emsg` and it is added to an
 805 accumulated set of candidate minimal protection sets.

806 **Step 4:** We verify whether `emsgs emsg` is minimal or further reduce the size
 807 by removing elements of a candidate set one by one and checking whether the result
 808 intersects every attack set.

809 To illustrate our algorithm, consider the attack sets in Equation 1. We first order
 810 the set of attack sets into a list according to its size. This leads to the list:

$$[\{\text{msg}_2\}, \{\text{msg}_4\}, \{\text{msg}_1, \text{msg}_2\}, \{\text{msg}_1, \text{msg}_3, \text{msg}_5\}]$$

811 We then start removing from this list any attack set that is a superset of another attack
 812 set in the list. For example, the attack set $\{\text{msg}_1, \text{msg}_2\} \supset \{\text{msg}_2\}$ and therefore it is
 813 removed. It results in the following list

$$\mathcal{A}_L = [\{\text{msg}_2\}, \{\text{msg}_4\}, \{\text{msg}_1, \text{msg}_3, \text{msg}_5\}]$$

814 Now we start with the pair $[\emptyset, \mathcal{A}_L]$. Pick a message that appears in the most attack sets
 815 in \mathcal{A}_L . In the case above, any message will do as all messages appear once. Say we
 816 picked `msg4`. This results in the pair:

$$[\{\text{msg}_4\}, [\{\text{msg}_2\}, \{\text{msg}_1, \text{msg}_3, \text{msg}_5\}]]$$

817 The algorithm continues by picking say `msg5` leading to the pair:

$$[\{\text{msg}_4, \text{msg}_5\}, [\{\text{msg}_2\}]]$$

818 and finally msg_2 , returning the minimal set:

$$\{\text{msg}_2, \text{msg}_4, \text{msg}_5\}.$$

819 The algorithm computes a protection set that contains at least one message of each
820 given attack set. The protection set computed is minimal as we check that removing
821 any element would enable an attack.

822 **Theorem 4.2.** *The algorithm described above results in a minimal protection set.*

823 **Proof.** The algorithm input I is $\text{all}\mathcal{A}[n]$ the set of attack message sets of size at most
824 n . A protection set for I is a set of messages such that if the intruder is unable to send
825 any of these messages, no attack in I can be carried out.

The algorithm has three stages: (1) converting the input to a list

```
asetSetsLp = pruneEMsgss (emsgsSet2emsgsList (asetSets));
```

826 (2) computing refinement sequences of partial protection sets $[\text{emsgs}_i, \text{emsgssl}_i]$
827 by adding a message in $\text{maxOcc}(\text{emsgssl}_i)$ to emsgs_i and removing it from all
828 message sets of emsgssl_i until there are no more messages to remove; (3) removing
829 redundant messages from the resulting protection sets.

830 1. Claim: A message set emsgs is a protection set for the input I iff it has non-
831 empty intersection with each message set in asetSetsLp .

832 By construction, if emsgs is an attack set of I of size $j+1$ then either emsgs is an
833 element of $\text{asetSetsLp}[j]$ or there is some $i < j$ and emsgs0 in $\text{asetSetsLp}[i]$
834 that is contained in emsgs . Furthermore, if emsgs is an element of $\text{asetSetsLp}[j]$
835 then for $i < j$ no emsgs0 in $\text{asetSetsLp}[i]$ is a subset of emsgs .

836 (Forward implication) Suppose emsgs is a protection set and there is some emsgs0
837 in asetSetsLp that has empty intersection with emsgs . Since emsgs0 is an attack
838 set and all its element are available to the attacker, emsgs can not be a protection set
839 for I .

840 (Backward implication) Suppose emsgs has non-empty intersection with each
841 message set in asetSetsLp . If there is an attack it must use $\text{emsgsA} - \text{emsgs}$
842 for some emsgsA in I . This is another attack set and is either in asetSetsLp or
843 contains some message set from asetSetsLp which intersects emsgs . A contradic-
844 tion.

845 Thus Claim 1 is proved.

2. We claim stage 2 produces a (finite) tree of partial protection sets such that
the message set of the leaves are protection sets for the I . In particular for each
node, $[\text{emsgs}, \text{emsgssl}]$, of the tree if emsgs1 intersects every set of emsgssl
then $\text{emsgs} \cup \text{emsgs1}$ intersects every message set of asetSetsLp (recall the root).
Clearly this holds for the root of the tree, $[\text{none}, \text{asetSetsLp}]$. Assume the claim
holds for a node $[\text{emsgs}, \text{emsgssl}]$. Its children have the form

$$[\text{emsgs}, \text{emsg}, \text{emsgssl}/\text{emsg}]$$

846 where $\text{emsg} \in \text{maxOcc}(\text{emsgssl})$ and $\text{emsgssl}/\text{emsg}$ is the result of remov-
847 ing emsg from each message set of emsgssl (and removing empty sets). Thus if

Table 2: Number of messages that are signed by the Naive Security Wrappers and the Refined Security Wrapper

Case	PnP	2PnP	PnP-2Msgs	2PnP-2Msgs
Naive	3	3	7	14
Refined	1	1	3	6

848 `emsgs1` intersects each (non-empty) message set of `emsgssl/emsg` then the set
 849 `emsgs1`, `emsg` intersects each (non-empty) message set of `emsgssl` since if a mes-
 850 s-age set of `emsgssl` does not intersect `emsgs1` it must be because it was removed
 851 by `emsg` and hence intersects with `emsg`. Clearly the tree is finite, since the branches
 852 have finite choices and at each level the second component gets smaller. Thus Claim 2
 853 is proved.

854 Finally, stage 3 just removes messages that can be eliminated with out violating the
 855 intersection property, to produce minimal protection sets.

856 Note that the algorithm `genMinProts` is sound (by the above proposition) but is
 857 not complete. It will generate some minimal protection sets, but there may be some
 858 that it misses. If completeness is more important than efficiency, the algorithm can be
 859 modified to consider every message that occurs in some set in `emsgssl` rather than
 860 restricting attention to messages in `mxOcc(emsgssl)`. This will be, however, less
 861 efficient.

862 We applied our algorithm to the the four scenarios presented in Section 4. The
 863 results are summarized by Table 2. `PnP` and `2PnP` have pruned attack sets of size 1
 864 for bounds up to 3. Thus the union of these sets is the minimal protection set. For
 865 scenarios `PnP-2Msgs` and `2PnP-2Msgs`, pruned attack sets are of size 2 and there is
 866 a single minimal protection set. In the `PnP-2Msgs` scenario the naive protection set
 867 has size 7, and the minimal protection set has size 3. In the `2PnP-2Msgs` scenario the
 868 naive protection set has size 14, and the minimal protection set has size 6.

869 5. Related Work

870 There are a number of recent reports concerning the importance of cybersecurity
 871 for Industry 4.0. Two examples are the German Federal Office for Information Security
 872 (BSI) commissioned report on OPC UA security [12], and the ENISA study on good
 873 practices for IoT security [10]. OPC Unified Architecture (OPC UA) is a standard for
 874 networking for Industry 4.0 and includes functionality to secure communication. The
 875 BSI commissioned report describes a comprehensive analysis of security objectives
 876 and threats, and a detailed analysis of the OPC UA Specification. The analyses are
 877 informal but systematic, following established methods. A number of ambiguities and
 878 issues were found in this process. The ENISA report provides guidelines and security
 879 measures especially aimed at secure integration of IoT devices into systems. It includes

880 a comprehensive review of resources on Industry 4.0 and IoT security, defines concepts,
881 threat taxonomies and attack scenarios. Again, systematic but informal.

882 Although there is much work on modeling cyber physical systems and cyber phys-
883 ical security (see [17] for recent review), much of it is based on simulation and testing.
884 The formal modeling work focuses on general CPS and IoT not on the issues specific
885 to I4.0 type situations. Lanotte *et al.* [15] propose a hybrid model of cyber and phys-
886 ical systems and associated models of cyber-physical attacks. Attacks are classified
887 according to target device(s) and timing characteristics. Vulnerability to a given class
888 is assessed based on the trace semantics. A measure of attack impact is proposed along
889 with a means to quantify the chances of success. The proposed model is much more
890 detailed than our model, considering device dynamics, and is focussed on traditional
891 control systems rather than IoT in an Industry 4.0 setting. The work in [24] relates to
892 our work in proposing a method using formal methods to find all attacks on a system
893 given possible attacker actions. The authors do not propose mitigations. SOTERIA
894 [6] is a tool for evaluating safety and security of individual or collections of IoT appli-
895 cations. It uses formal methods to verify properties of abstract models of applications
896 derived automatically from code (of suitable form). It requires access to the application
897 source code.

898 Several mature tools based on formal methods, such as TAMARIN [19], Maude-
899 NPA [11], ProVerif [5] and OFMC [4], have been applied for the verification of secu-
900 rity protocols. These works are based on similar symbolic techniques used here, such
901 as modeling intruder symbolically following the Dolev-Yao intruder model [9]. The
902 application here is different as we verify embedded systems and not communication
903 protocols. This impacts the type of analyses that are required. For example, the types
904 of event messages transmitted between devices is far simpler than the messages trans-
905 mitted in security protocols. Moreover, as Industry 4.0 applications are cyber-physical
906 systems, safety becomes important. Therefore, the main goal is not to preserve the
907 confidentiality of some data, but to guarantee the safety of the system even in the pres-
908 ence of intruders. The formal model proposed here reflects this as it takes as input not
909 the messages that shall be confidential, but system configurations that are hazardous.
910 Finally, it is not clear whether existing tools can be used to recommend policies for
911 security wrappers as done by the machinery proposed in this paper.

912 The MBSE tool TTool [3] provides automated support for security verification us-
913 ing ProVerif. It is to the best of our knowledge the only MBSE tool integrated with
914 formal security verification tools. Following an MBSE approach, system specification
915 uses function blocks whose behavior are specified using activity diagrams. It imple-
916 ments a model to model translation [2] from TTool specification to ProVerif speci-
917 fications enabling the verification of security properties, such as confidentiality and
918 authenticity. As with ProVerif, TTool does not support the use of formal verification to
919 identify how intruders can lead to harm neither support automated methods to construct
920 security wrappers.

921 The complexity of periodic system such as those used in Industry 4.0 has been sub-
922 ject of the paper [1]. It has been shown that if the intruder is not bounded, reachability
923 problems are undecidable. Moreover, the same problems are PSPACE-complete if the
924 intruder is bounded. This paper complements the existing work by demonstrating that
925 existing methods can be used in realistic size application, such as the PnP.

926 The idea of using theory transformations to relate the application, system level
927 specifications and reduce many reasoning problems to reasoning at the application
928 level is based on the notion of formal patterns reviewed in [20]. An early example
929 of wrapping to achieve security guarantees is presented in [7] to mitigate DoS attacks.

930 **6. Conclusions and Future Work**

931 This paper presents a formal framework in rewriting logic for exploring I4.0 (smart
932 factory) application designs and a bounded intruder model for security analysis. The
933 framework provides functions for enumerating message injection attacks, and generat-
934 ing policies mitigating such attacks. It provides theory transformations from applica-
935 tion specifications to specifications of systems with application components executing
936 on devices, and for wrapping devices to protect against attacks using the generated
937 policies. Theorems relating different specifications and showing preservation of key
938 properties are given. We believe that formal executable models can be valuable to sys-
939 tem designers to find corner cases and to explore tradeoffs in design options concerning
940 the cost and benefits of security elements.

941 Future work includes theory transformations to refine the system level model to a
942 network model with multiple subnets and switches, adding timing and modeling con-
943 straints induced by use of the TSN network protocol. As in our previous work [13], we
944 are investigating the complexity of security properties given intruder models weaker
945 than the traditional Dolev-Yao intruder [9]. We are also considering increasing the
946 expressiveness of function block specifications to include time constraints as in [14]
947 to automate the verification of properties based on time trace equivalence [23], such
948 as privacy attacks. Finally, since these devices have limited resources, they may be
949 subject to DDoS attacks. Symbolic verification can be used to check for such vulnera-
950 bilities [26].

951 Another important direction is developing theory transformations for correct-by-
952 construction distributed execution [16]. This means accounting for real timing con-
953 siderations and network protocols, and identifying conditions under which application
954 and system level properties are preserved. An important use of the framework that
955 we intend to investigate is relating safety and security analyses and connecting formal
956 analyses to the engineering notations used for safety and security.

957 We are also currently extending our implementation to support the automated ex-
958 ploration of mappings of function blocks to devices. In particular, we are investigating
959 the extension of [25] to take into account security objectives in addition to device per-
960 formance limitations, device capabilities, and deadlines.

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